Latent-factor models (LFM) based on collaborative filtering (CF), such as matrix factorization (MF) and deep CF methods, are widely used in modern recommender systems (RS) due to their excellent performance and recommendation accuracy. Notwithstanding their great success, in recent years, it has been shown that these methods are vulnerable to adversarial examples, i.e., subtle but non-random perturbations designed to force recommendation models to produce erroneous outputs. The main reason for this behavior is that user interaction data used for training of LFM can be contaminated by malicious activities or users’ misoperation that can induce an unpredictable amount of natural noise and harm recommendation outcomes. On the other side, it has been shown that these systems, conceived originally to attack machine learning applications, can be successfully adopted to strengthen their robustness against attacks as well as to train more precise recommendation engines.

In this respect, the goal of this survey is two-fold: (i) to present recent advances on AML-RS for the security of RS (i.e., attacking and defense recommendation models), (ii) to show another successful application of AML in generative adversarial networks (GANs), which use the core concept of learning in AML (i.e., the min-max game) for generative applications.

In this survey, we provide an exhaustive literature review of 60 articles published in major RS and ML journals and conferences. This review serves as a reference for the RS community, working on the security of RS and recommendation models leveraging generative models to improve their quality.

ACM Reference Format:

1 INTRODUCTION
In the age of data deluge, where users are facing a new form of information explosion, recommender systems (RS) have emerged as a paradigm of information push to lessen decision anxieties and
consumer confusion by over-choice. RS enhance users' decision-making process and support sales\(^1\) by personalizing item recommendations for each user and helping them discover novel products. RS are a pervasive part of user experience online today and serve as a principal choice for many consumer-oriented companies such as Amazon [102, 106], Netflix [43], Google (e.g., YouTube [149]). Among different types of recommendation techniques, collaborative filtering (CF) methods have been the mainstream of recommendation research both in academia and industry due to their superb recommendation quality. CF builds on the fundamental assumption that users who have expressed similar interests in the past, will maintain similar choices in future [42], and infers target user preference over unseen items by leveraging behavioral data of other users and exploiting similarities in their behavioral patterns. In the following, we summarize the progress in CF-model developments over the last three decades.

Milestones in CF models over the past decades are depicted in Figure 1. The core idea of a recommending service can be traced back to cognitive science first described in a system named Grundy in 1972 [94] where the authors used stereotypes to build user models and suggest relevant books to individual users. Almost 20 years later, the idea of recommender systems started booming. In 1992, Belkin et. al. [5] discussed the component of an information filtering (IF) system in comparison with an information retrieval (IR) system.\(^2\) Afterwards, several works made attempts to automate the idea of CF, notably, the first CF model made in 1992 by Goldberg et al. Tapestry [42] — which consolidated the idea of like-minded users as the principal mechanism of CF — GroupLens in 1994 [93], the Bellcore’s video recommender in 1995 [54] and the music and album recommender Ringo in 1998 [101].

\(^1\)It has been known that RS are an important monetization method of businesses. For instance, 80% of hours streamed at Netflix derives from recommendation [43], 8% of Amazon traffics derives from its recommendation engine [106].

\(^2\)The work by Belkin et. al. [5] used/assumed content-based filtering (CBF) system as the primary example of an IF system in which the CBF systems uses only textual information. Against this traditional view, modern RS nowadays utilize a variety of other information such as linked open data (LOD), multimedia (audio and visual) features, user-generated content (UGC) and heterogeneous information networks [76].

Under Review
We can identify two major eras in the development of CF models based on their main objective:

1. The era focused on maximizing/enhancing the recommendation accuracy and beyond-accuracy;
2. The post-neural era, the transition era from classical learning to adversarial machine learning.

**Accuracy maximization and beyond-accuracy enhancement era.** In this era, the main effort of research and practitioner-scholars was concentrated on the “golden objective” of maximizing recommendation accuracy. Consequently, machine-learned models tend to use any available signal in the data to reach this goal, even though some of the data contained noise as the results of users’ misoperations. We distinguish between three classes of CF techniques in this era: (i) classical non-neural CF era, (ii) domain/task-dependent CF era and, (iii) deep neural CF era, each described in the following.

- **Classical non-neural CF.** The starting of this era dates back to the 1990s and is still progressing. Over these three decades, the study on CF methods has been the subject of active research by the RS community resulting in a diverse set of models and evaluation measures to assess the effectiveness of these models. We can classify these CF approaches based on various dimensions. For example, from a learning paradigm perspective, CF models can be classified according to (i) memory-based CF and (ii) model-based CF models, in which the former category makes recommendation based on the similarity of users-user interactions (i.e., user-based neighborhood model) or item-item interactions (i.e., item-based neighborhood model) while the latter category predicts users’ feedback of unseen items using latent factor models such as matrix-factorization (MF) [63]. From the model training perspective, it is possible to categorize these models based on the loss functions employed according to (i) point-wise loss where the goal is to optimize towards a predefined ground-truth (e.g., matrix factorization approach based on SVD), (ii) pairwise ranking loss where the goal is to optimize personalized ranking (e.g., matrix factorization based on BPR) and (iii) list-wise loss where the objective is to reflect the distance between the reference list and the output list [104].

- **Domain-dependent CF.** “Recommendation is not a one-size-fits-all problem” [38]. The research in this era has the main focus to integrate a wealth of side information data beyond the user rating matrix (URM) into the recommendation models to make RS adapted in specific domains. Such data consist of side information of users (e.g., demographics, personality traits, social-network information), items (e.g., item content, attributes) and the interplay between them (e.g., the time of interaction). For example, in [83, 118] the authors use item description information such as textual metadata (e.g., movie cast, product review, artist information) and in [32, 117] features extracted directly from the signal (images or audio) to enhance recommendation. These approaches can also be used to alleviate cold-start issues such as data sparsity or new/item user problem, which impedes the performance of CF models. Based on the unique nature of side-information in different domains, different hybrid CF strategies have been developed [98, 103]. The survey [103] by Shi et al. provides a good frame of reference for CF methods leveraging rich side information.

- **Deep neural CF.** Another milestone is concerned with the success of deep learning (DL) or “neural” technology in machine learning (ML). DNNs have shown to be capable of providing remarkable accuracy in several predictive tasks and domains such as image classification [47] and speech recognition [96] among others. In the field of RS, DNNs have been shown useful for the recommendation in several ways such as extracting deep features (via using CNNs), modeling item content in CF models by integrating side item information, building CF models by parameterizing latent factor models into layers of a DNN (deep CF), and modeling sequential
Table 1. Collaborative-based Recommender Models.

<table>
<thead>
<tr>
<th>Recommender Abbr.</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Classical RS</strong></td>
<td></td>
</tr>
<tr>
<td>MF [63]</td>
<td>Matrix Factorization (MF) is the state-of-the-art recommendation model for implicit datasets.</td>
</tr>
<tr>
<td>BPR-MF [91]</td>
<td>Bayesian Personalized Ranking (BPR-MF) is a highly competitive MF-model for item recommendation optimized with a pairwise objective function (BPR).</td>
</tr>
<tr>
<td>FM [90]</td>
<td>Factorization Machine (FM) is a generalized MF model that encodes (users, items, features)-interactions into a joint dot-product space.</td>
</tr>
<tr>
<td>VBPR [50]</td>
<td>Visual Bayesian Pairwise Ranking (VBPR) model integrates items’ visual features — extracted by a CNN — in the BPR-MF preference prediction.</td>
</tr>
<tr>
<td><strong>Deep-Learning RS</strong></td>
<td></td>
</tr>
<tr>
<td>CDL [123]</td>
<td>Collaborative Deep Learning (CDL) is a hybrid model combines the extraction of deep items’ features with the collaborative user-item feedbacks.</td>
</tr>
<tr>
<td>AutoRec [99]</td>
<td>AutoRec reconstructs partial user profiles (i.e., item recommendation) based on the reconstruction power of auto-encoders .</td>
</tr>
<tr>
<td>CVAE [70]</td>
<td>Collaborative Variational Auto-Encoder (CVAE) performs recommendations by learning both deep user-item latent representations from content data and implicit user-item relationships from both content and ratings.</td>
</tr>
<tr>
<td>RRN [131]</td>
<td>Recurrent Recommender Networks (RRN) predicts future user preferences by integrating MF with a Long Short-Term Memory (LSTM) model to capture dynamics.</td>
</tr>
<tr>
<td>NCF [52]</td>
<td>Neural Collaborative Filtering (NCF) learns user-item preference function by replacing the inner product of MF with a neural architecture to extract non-linear relations.</td>
</tr>
</tbody>
</table>

relations (via using RNNs). As for deep-CF approaches, while MF assumes that the linear interaction between user and item latent factors can explain observed feedback, deep CF models can model a more complex representation of hidden latent factors by parametrization of MF via a DNN. Table 1 summarizes the list of state-of-the-art classic and neural-CF approaches used for different recommendation tasks.

A summary of the most relevant approaches [31] is presented in Table 1.

The post neural era, the transition era from classical learning to adversarial machine learning. Despite the significant success of DNNs to solve a variety of complex prediction tasks on non-structured data such as images, recently, they have been demonstrated to be vulnerable to adversarial examples. Adversarial examples (or adversarial samples) are subtle but non-random perturbations designed to dictate a ML model to produce erroneous outputs (e.g., to misclassify an input sample). The subject started booming after the pioneering work [111] by Szegedy et al. reported the vulnerability of DNNs against adversarial samples for the image classification task. It has been shown that by adding a negligible amount of adversarial perturbation on an image (e.g., a panda), a CNN classifier could misclassify the image in another class (e.g., a gibbon) with high confidence. These results were quite shocking since it was expected that state-of-the-art DNNs that generalize well on unknown data do not change the label of a test image that is slightly perturbed and is human-imperceptible. Algorithms that aim to find such adversarial perturbations are referred to as adversarial attacks. As ML models are involved in many consumer safety and security-intensive tasks such as autonomous driving, facial recognition, and camera surveillance, adversarial attacks pose significant concerns to the security and integrity of the deployed ML-models.

In the field of RS, numerous works have reported the failure of machine-learned recommendation models, i.e., latent-factor models (LFM) based on CF like MF and deep CF methods widely adopted in modern RS, against adversarial attacks. For instance, in [51] He et al. showed that by exposing the model parameters of BPR [91] to both adversarial and random perturbations of the BPR model
parameters, the value of nDCG is decreased by -21.2% and -1.6% respectively, which is equal to a staggering impact of approximately 13 times difference. One main explanation for such behavior is that adversarial attacks exploit the imperfections and approximations made by the ML model during the training phase to control the models’ outcomes in an engineered way [85].

Adversarial machine learning (AML) is an emerging research field that combines the best practices in the areas of ML, robust statistics, and computer security [115, 134]. It is concerned with the design of learning algorithms that can resist adversarial attacks, studies the capabilities and limitations of the attacker, and investigates suitable countermeasures to design more secure learning algorithms [56]. The pivotal distinguishing characteristic of AML is the notion of “min-max” game, in which two competing players play a zero-sum differential game, one — i.e., the attacker — tries to maximize the likelihood of the attack success, while the other — i.e., the defender — attempts to minimize the risk in such a worst-case scenario. In the context of RS, the defender players can be a machine-learned model such as BPR or a neural network, while the attacker is the adversarial model.

To protect models against adversarial attacks, adversarial training has been proposed. It is a defensive mechanism whose goal is not to detect adversarial examples, instead to build models that perform equally well with adversarial and clean samples. Adversarial training consists of injecting adversarial samples —generated via a specific attack model such as FGSM [45] or BIM [65]— into each step of the training process. It has been reported —both in RS [112] and ML [130]— that this process leads to robustness against adversarial samples (based on the specific attack type on which the model was trained on), and better generalization performance on clean samples. For instance, in [112], the authors show that the negative impact of adversarial attacks measured in terms of nDCG is reduced from -8.7% to -1.4% when using adversarial training instead of classical training.

The above discussion highlights the failure of classical ML models (trained on clean data) in adversarial settings and advocates the importance of AML as a new paradigm of learning to design more secure models. Nevertheless, the attractiveness of AML that exploits the power of two adversaries within a “min-max” game is not limited to security applications and has been exploited to build novel generative models, namely generative adversarial networks (GANs). The key difference is as follows: the models used in AML for security (or attack and defense) focus only on a class of discriminative models (e.g., classifiers), whereas GANs build upon both discriminative and generative models. A GAN is composed of two components: the generator $G$ and the discriminator $D$. The training procedure of a GAN is a min-max game between $G$, optimized to craft fake samples such that $D$ cannot distinguish them from real ones, and $D$, optimized to classify original samples from generated ones correctly. Through the interplay between these two components, the model reaches the Nash equilibrium where $G$ has learned to mimic the ground-truth data distribution, e.g., a profile of a particular user. In the present survey, we identified different application for GAN-based RS that include, improving negative sampling step in learning-to-rank objective function [39, 126], fitting the generator to predict missing ratings by leveraging both temporal [8, 147] and side-information [18, 125], or augmenting training dataset [17, 37].

1.1 Main results

The focus of this survey is on the following two studies both using the concept of “min-max” in their formulation:

(1) **AML for the security of RS**: This is the “principal application” of AML in RS, which focuses on adversarial attacks and defense models in RS. We present it in Section 2.
(2) *Application of AML in GANs*: This is a “derived topic” from AML, that is focused on “generative” learning models. We identified four types of applications in this category, namely: improving CF recommendation, context-aware recommendation, cross-domain recommendation and complementary recommendation, which we present in Section 3.

Overall, AML-based recommendation scenarios are highly relevant to the field of RS. Indeed, in recent years, a growing number of relevant research works have been proposed. Despite this success, research in AML-RS is overly scattered with each paper focusing on a particular task, domain, or architecture. One major objective of this survey is to categorize state-of-the-art research in the field based on several identified dimensions in order to provide a richer understanding of the different facets of the AML-RS. Our ultimate motivation is to lay the foundation for a more standardized approach for reproducible research works in the field.

The practical outcome of the present survey includes:

(1) To the best of our knowledge, this is the first work that provides a comprehensive understanding of AML in RS domain, unifying the advances made in the communities of ML and RS;

(2) This survey sheds lights on two successful applications of AML, namely: adversarial attacks and defenses and GANs, both using the concept of “min-max” game at their core. It provides an extensive literature review of the existing research, specifically:

- For AML-based RS focused on security: we present a unified problem formulation and discuss the existing adversarial attack studies on RS from various perspectives in particular attack and defense models, recommendation dimensions as well as evaluation and attack metrics used in different papers.

- For GAN-based RS, we provide a conceptual view of recommendation approaches incorporating GAN to address the item recommendation task and we review an extensive number of research, which we classify according the generator, discriminator type and training paradigm. We also categorize the existing research into several distinctive high-level goals (e.g., complementary recommendation in fashion domain, context-aware recommendation, etc.).

(3) We created an open-source repository\(^3\) that includes all reviewed research articles which is updated over time. The aim of this repository is to facilitate bench-marking AML in the RS field by proving the released codes links and datasets used for the evaluation.

To identify the relevant publications that constitute the state-of-the-art on adversarial learning in recommender systems, we mainly relied on publications indexed in major computer science bibliography databases namely DBLP (https://dblp.uni-trier.de/) and Scopus (https://www.scopus.com). In addition, realizing the fact that many top-tiers venues also publish related works, which may not be necessarily indexed in the above databases, we also gathered a number of related publications by searching directly through Google Scholar (https://scholar.google.it/). Our search strategy was composed of two main stages:

(1) relevant publication collection,

(2) filtering and preparing the final list.

We collected also referenced publications in the yet selected ones. As for the first stage, we queried the term “adversarial recommend” in the above-mentioned indexing services. While search in DBLP returns publications containing the query term in the title, the search results from Scopus and

\(^{3}\)Table with AML-RS publications at https://github.com/sisinflab/adversarial-recommender-systems-survey

Under Review
Table 2. List of abbreviations used throughout this paper.

<table>
<thead>
<tr>
<th>Abbreviation</th>
<th>Term</th>
</tr>
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<tbody>
<tr>
<td>AI</td>
<td>Artificial Intelligence</td>
</tr>
<tr>
<td>AML</td>
<td>Adversarial Machine Learning</td>
</tr>
<tr>
<td>C&amp;W</td>
<td>Carlini and Wagner</td>
</tr>
<tr>
<td>CA</td>
<td>Context-Aware RS</td>
</tr>
<tr>
<td>CBF-RS</td>
<td>Content-Based Filtering RS</td>
</tr>
<tr>
<td>CF-RS</td>
<td>Collaborative Filtering RS</td>
</tr>
<tr>
<td>CS</td>
<td>Cold start</td>
</tr>
<tr>
<td>CD-RS</td>
<td>Cross-Domain RS</td>
</tr>
<tr>
<td>CV</td>
<td>Computer Vision</td>
</tr>
<tr>
<td>DL</td>
<td>Deep Learning</td>
</tr>
<tr>
<td>DNN</td>
<td>Deep Neural Network</td>
</tr>
<tr>
<td>ERM</td>
<td>Empirical Risk Minimization</td>
</tr>
<tr>
<td>FGSM</td>
<td>Fast Gradient Sign Method</td>
</tr>
<tr>
<td>FNCF</td>
<td>Feature-based Neural Collaborative Filtering</td>
</tr>
<tr>
<td>GAN</td>
<td>Generative Adversarial Network</td>
</tr>
<tr>
<td>G-RS</td>
<td>Graph-based RS</td>
</tr>
<tr>
<td>IR</td>
<td>Information Retrieval</td>
</tr>
<tr>
<td>LFM</td>
<td>Latent Factor Model</td>
</tr>
<tr>
<td>LSTM</td>
<td>Long Short-Term Memory</td>
</tr>
<tr>
<td>MF</td>
<td>Matrix Factorization</td>
</tr>
<tr>
<td>ML</td>
<td>Machine Learning</td>
</tr>
<tr>
<td>nDCG</td>
<td>Normalized Discounted Cumulative Gain</td>
</tr>
<tr>
<td>RS</td>
<td>Recommender Systems</td>
</tr>
<tr>
<td>SM</td>
<td>Social Media</td>
</tr>
<tr>
<td>SN</td>
<td>Social Network</td>
</tr>
<tr>
<td>URM</td>
<td>User Rating Matrix</td>
</tr>
</tbody>
</table>

Google Scholar return publications containing the query *both in the tile and the content*, thereby altogether forming a complete list of identified research works. We collected all resulting publications from DBLP, Scopus and Google Scholar search. In the second stage, we went through all the collected research works and removed all irrelevant works. These for instance could include works that used AML for an application different than RS (e.g., in Computer Vision [111], Speech Enhancement [87]). We mostly turned our attention to conference-level and journal publications published in top conferences and to a lesser extent to workshop publications or works published in entry-level venues. Some of the considered journals and conferences include: the ACM Conference on Recommender Systems (RecSys), the International ACM SIGIR Conference on Research and Development in Information Retrieval (SIGIR), the ACM International Conference on Web Search and Data Mining Conference (WSDM), the International World Wide Web Conference (TheWebConference), the International Joint Conferences on Artificial Intelligence (IJCAI), and the Knowledge Discovery and Data Mining conference (KDD).

Part of the material presented in this survey has been presented as a tutorial at the WSDM’20 conference [35].

In the subsequent core section of this survey, we present adversarial learning for attacking and defending RS in Section 2, AML for GAN-based RS in Section 3. Section 4 presents the open research directions and concludes the survey.

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4 Tutorial slides at https://github.com/sisinflab/amlrecsys-tutorial
2 ADVERSARIAL MACHINE LEARNING FOR SECURITY OF RS

For security concerns to be addressed appropriately in today’s ML systems, there is a need to bridge the knowledge gap between the ML and computer security communities. Adversarial machine learning (AML) is a recently proposed and popularized approach that lies at the intersection of the above fields combining the best works of the two. The main goal of AML for security is to build systems that can learn in normal conditions and such that when they are under attack—in particular under adversarial attack—they can respond rapidly and safeguard ML models against emerging adversaries’ threats.

As the literature on AML for security emerged in the context of ML, in Section 2, we first discuss the fundamentals of attacks on, and defenses of ML models (cf. Section 2.1). We then present AML-based RS focused on security applications in which we survey various identified literature in the field and classify them based on several methodological and evaluation-related dimensions (cf. Section 2.2).

2.1 Attack and Defense in ML and RS

Throughout this section, we consider a supervising learning — classification — task. Assume a training dataset \( D \) of \( n \) pairs \((x, y) \in X \times Y\), where \( x \) is the input sample, and \( y \) is its corresponding class label. The problem of classification is formulated as finding a candidate function \( f_\theta : X \rightarrow Y \) that can predict the class label \( y \) around the input sample \( x \), where \( \theta \) is the model parameter. This leads to solving an empirical risk minimization (ERM) problem of the form

\[
\min_\theta \sum_{(x_i, y_i) \in D} \ell (f(x_i; \theta), y_i)
\]

where \( \ell (.) \) is the empirical risk function (the loss function). Various adversarial attacks aim to find a non-random perturbation \( \delta \) to produce an adversarial example \( x_{\text{adv}} = x + \delta \) that can cause an erroneous prediction (e.g., misclassification) as we will see in the following section.

2.1.1 Attacks

In recent years, the advances made in deep learning (DL) have considerably advanced the intelligence of ML models in a unique number of predictive tasks such as classification of images and other unstructured data. Notwithstanding their great success, recent studies have shown that ML/DL models are not immune to security threats from adversarial use of AI. We can classify attacks against a ML model along three main dimensions, attack timing and goal.

Attack timing. As illustrated in Fig. 2, an adversary can attack a ML model at two main stages of the learning pipeline, during training or production. These two categories of attacks are respectively known as (i) training-time attack (a.k.a. causative or poisoning attack) [9] and, ii) inference-time attack (a.k.a. exploratory or evasion attack) [111].

- Poisoning attack. Data poisoning attacks are realized by injecting false data points into the training data with the goal to corrupt/degrade the model (e.g., the classifier). Poisoning attacks have been explored in the literature for a variety of tasks [120], such as (i) attacks on binary classification for tasks such as label flipping or against kernelized SVM, (ii) attacks on unsupervised learning such as clustering and anomaly detection and, (iii) attacks on matrix completion task in RS known as shilling attacks [33, 34]. As an example, in the pioneering work [9], Biggio et al., propose a poisoning attack based on properties of the SVM optimal solution that could significantly degrade the classification test accuracy.
• *Evasion attack*. Unlike poisoning attacks, evasion attacks do not interfere with training data. They adjust malicious samples during the inference phase. These attacks are also named *decision-time* attacks referring to their attempt to *evoke* the decision made by the learned model at test time. Evasive attacks are conducted by crafting adversarial examples — subtle but non-random perturbation — added to original data to cause the learned model to produce erroneous output. Adversarial examples are additive perturbations of the input sample under a norm constraint whose goal is to fool the target model (e.g., a classifier or a recommendation model). Perturbations are optimized by an attack algorithm known as *adversarial attack* against the target model.

**Attack goal.** Attacks are conducted for different goals. We can distinguish between two main classes of attack goals: i) *untargeted attack* and, ii) *targeted attack*. To provide the reader with an intuitive insight of the mechanism behind adversarial attacks and defense strategies, we define them formally for a *classification* task [120].

The goal of the attacker in *untargeted adversarial attack* (misclassification) is to add a minimal amount of perturbation $\delta$ on the input sample $x$ such that it can cause incorrect classification.

**Definition 2.1 (Untargeted adversarial attack).** Given $f(x; \theta) = y$, an Untargeted Adversarial Attack is formulated as:

$$\min_{\delta} \|\delta\| \quad \text{s.t.} \quad f(x + \delta; \theta) \neq y, \; x + \delta \in [0,1]^n$$  \hspace{1cm} (1)

The second constraint $x + \delta \in [0,1]^n$ is a value-clipping constraint needed for images, to bound the adversarial samples into a predefined range so that the images remain visible after adversarial attack. Alternatively, we can formulate the problem as an *unconstrained optimization* problem where the goal of the attacker is to maximize the loss between the perturbed sample $x + \delta$ and true class $y$

$$\max_{\delta: \|\delta\| \leq \epsilon} \ell(f(x + \delta; \theta), y)$$  \hspace{1cm} (2)
Obviously since adding an unbounded amount of noise on the input will eventually lead to a classification error, the goal of the attacker is to minimize a norm-constrained form of noise, that is $\|\delta\| \leq \varepsilon$ for some exogenously given $\delta$.

In the context of DNN, the above attacks are categorized based on the norm used to represent the magnitude of the noise according to the following norm types \[120\]: $l_0$, $l_1$ and $l_2$ and $l_\infty$.

**Definition 2.2 (Targeted adversarial attack).** The goal of the attacker in targeted adversarial attack is to perturb the input by adding a minimum amount of perturbation $\delta$ such that it can force the model to misclassify the perturbed sample into an illegitimate target class. Given $f(x; \theta) = y$, with $y \neq y_t$, we formulate the problem as:

$$\min_{\delta} \|\delta\| \quad \text{s.t.:} \quad f(x + \delta; \theta) = y_t$$

(3)

Similarly, the above problem can be expressed as a unconstrained optimization problem

$$\min_{\delta: \|\delta\| \leq \varepsilon} \delta \ell(f(x + \delta; \theta), y_t)$$

(4)

The most common attack types so far exploited in the community of RS are fast gradient sign attack (FGSM) \[45\] and Carlini and Wagner (C&W) attacks, which belong to $l_\infty$- and $l_2$-norm attack types respectively. We provide the formal definition of the FGSM and C&W attacks here.

**Definition 2.3 (FGSM attack).** The fast gradient sign method (FGSM) \[45\] utilizes the sign of the gradient of the loss function to find perturbation that maximizes the training loss (for untargeted case)

$$\delta = \varepsilon \cdot \text{sign}(\nabla_x \ell(f(x; \theta), y))$$

(5)

where $\varepsilon$ (perturbation level) represents the attack strength and $\nabla_x$ is the gradient of the loss function w.r.t. input sample $x$. The adversarial example is generated as $x^{adv} = x + \delta$. FGSM applies an $l_\infty$-bound constraint $\|\delta\|_{\infty} \leq \varepsilon$ with the original idea to encourage perceptual similarity between the original and perturbed samples. The unconstrained FGSM aims to find perturbation that would increase/maximize the loss value. The corresponding approach for targeted FGSM \[65\] is

$$\delta = -\varepsilon \cdot \text{sign}(\nabla_x \ell(f(x; \theta), y_t))$$

(6)

where the goal is to maximize the conditional probability $p(y_t|x)$ for a given input $x$.

Several variants of the FGSM has been proposed in the literature \[21, 130\]. For instance, the fast gradient value (FGV) method \[95\], which instead of using the sign of the gradient vector in FGSM, uses the actual value of the gradient vector to modify the adversarial change, or basic iterative method (BIM) \[65\] (a.k.a iterative FGSM) that applies FGSM attack multiple times iteratively using a small step size and within a total acceptable input perturbation level.

**Definition 2.4 (C&W attack).** The Carlini and Wagner (C&W) attack \[16\] is one of the most effective attack models. The core idea of C&W attack is to replace the standard loss function — e.g., typically cross-entropy — with an empirically-chosen loss function and use it in an unconstrained optimization formulation given by

$$\min_{\delta} \|\delta\|^p_p + c \cdot h(x + \delta, y_t)$$

(7)

where $h(\cdot)$ is the candidate loss function.
The C&W attack has been used with several norm-type constraints on perturbation \(l_0, l_2, l_{\infty}\) among which the \(l_2\)-bound constraint has been reported to be most effective [14, 15, 23].

**Adversarial attacks on RS - challenges and differences with ML tasks.** In spite of the similarities between ML classification and recommendation learning tasks, there are considerable differences/challenges in adversarial attacks on RS compared with ML and the degree to which the subject has been studied in the respective communities:

- **Poisoning vs. adversarial attack.** In the beginning, the main focus of RS research community has been on *hand-engineered* fake user profiles (a.k.a shilling attacks) against rating-based CF [33]. Given a URM with \(n\) real users and \(m\) items, the goal of a shilling attack is to augment a fraction of malicious users \([\alpha n]\) (\([\cdot]\) is the floor operation) to the URM \((\alpha \ll 1)\) in which each malicious use profile can contain ratings to a maximum number of \(C\) items. The ultimate goal is to harvest recommendation outcomes toward an illegitimate benefit, e.g., pushing some targeted items into the top-\(K\) list of users for market penetration. Shilling attacks against RS have an established literature and their development face two main milestones: the first one —since the early 2000s— where the literature was focused on building hand-crafted fake profiles whose rating assignment follow different strategy according to random, popular, love-hate, bandwagon attacks among others [10, 46]; the second research direction started in 2016 when the first ML-optimized attack was proposed by Li et al., [67] on factorization-based RS. This work reviews a novel type of data poisoning attack that applies the adversarial learning paradigm for generating poisoning input data. Nonetheless, given their significant impact against modern recommendation models, the research works focusing on *machine-learned adversarial attacks* against RS have recently received great attention from the research community.

- **CF vs. classification models:** Attacks against classification tasks focus on enforcing the wrong prediction of individual instances in the data. In RS, however, the mainstream attacks rely on CF principles, i.e., mining similarity in opinions of like-minded users to compute recommendations. This interdependence between users and items can, on the one hand, *improve robustness* of CF, since predictions depend on a group of instances not on an individual one and, on the other other hand, may cause *cascade effects*, where attack on individual user may impact other neighbor users [29].

- **Attack granularity and application type:** Adversarial examples created for image classification tasks are empowered based on continuous real-valued representation of image data (i.e., pixel values), but in RS, the raw values are user/item IDs and ratings that are discrete. Perturbing these discrete entities is infeasible since it may lead to changing the semantics of the input, e.g., loosely speaking applying \(ID + \delta\) can result in a new user \(ID\). Therefore, existing adversarial attacks in the field of ML are not transferable to the RS problems trivially. Furthermore, in the context of CV — attacks against images — the perturbations often need to be “human-imperceptible” or “inconspicuous” (i.e., may be visible but not suspicious) [130]. How can we capture these nuances for designing attacks in RS remains as an open challenge.

### 2.1.2 Defense against adversarial attacks

From a broad perspective, defense mechanisms against adversarial attacks can be classified as *detection* methods and methods seeking to increase the *robustness* of the learning model. The goal of this section is to briefly review approaches that build *robust ML* models in adversarial settings. The prominent methods used in RS are (i) the robust optimization and, (ii) the distillation method.
Robust optimization against adversarial attacks: At the heart of the robust optimization method is the assumption that every sample in the training data $D$ can be a source for adversarial behavior. It performs an ERM against a specific adversary on each sample in $D$ and applies a zero sum-game between the prediction and attack adversaries leading to the following robust optimization framework

$$\min_\theta \sum_{(x_i, y_i) \in D} \max_{\delta: \|\delta\| \leq \epsilon} \ell(f(x_i + \delta; \theta), y_i)$$

(8)

where $\epsilon$ is an upper-bound on the adversarial perturbation level $\delta$. The ultimate goal in robust optimization is that the prediction model will perform equally well with adversarial and clean inputs.

Definition 2.5 (Adversarial training). The goal of adversarial training is to build a robust model from ground-up on a training set augmented with adversarial examples. Adversarial regularization is one of the mostly investigated techniques for adversarial training, which utilizes an approximation of the worst-case loss function, i.e., $\max_{\delta: \|\delta\| \leq \epsilon} \ell(f(x + \delta; \theta), y_i)$, as the regularizer.

$$\ell_T = \min_\theta \sum_{i \in D} [\ell(f(x; \theta), y_i) + \lambda \max_{\delta: \|\delta\| \leq \epsilon} \ell(f(x + \delta; \theta), y_i)]$$

(9)

As it can be noted, the inner maximization finds the strongest attack against the prediction model that is subject to adversarial perturbation. The outer minimization estimates the strongest defensive against a given attack by giving up a level of accuracy due to the regularization. The parameter $0 < \lambda < 1$ controls the trade-off between accuracy (on clean data) and robustness (on perturbed data).

Example 1 (Adversarial training of BPR-MF). BPR is the state-of-the-art method for personalized ranking implicit feedbacks. The main idea behind BPR is to maximize the distance between positively and negatively rated items. Given the training dataset $D$ composed by positive and negative items for each user, and the triple $(u, i, j)$ (user $u$, a positive item $i$ and negative item $j$), the BPR objective function is defined as

$$\ell_{BPR}(D|\Theta) = \arg \max_\Theta \sum_{(u,i,j) \in D} \ln \sigma(\hat{x}_{ui}(\Theta) - \hat{x}_{uj}(\Theta)) - \lambda \|\Theta\|^2$$

(10)

where $\sigma$ is the logistic function, and $\hat{x}_{ui}$ is the predicted score for user $u$ on item $i$ and $\hat{x}_{uj}$ is the predicted score for user $u$ on item $j$; $\lambda \|\Theta\|^2$ is a regularization method to prevent over-fitting.5

Adversarial training of BPR-MF similar to Eq. 9 can be formulated as

$$\ell_{APR} = \min_\theta \sum_{(u,i,j) \in D} [\ell_{BPR}(D|\Theta) + \lambda \max_{\delta: \|\delta\| \leq \epsilon} \ell_{BPR}(D|\Theta + \delta)]$$

(11)

Under Review
2.2 Adversarial Machine Learning for Attack and Defense on RS

In this section, we focus on state-of-the-art approaches to the application of AML in RS research. RS which employ AML for security applications in recommendation tasks, follow the simplified steps sketched in Fig. 3. In the following, in addition to providing concise summaries of the surveyed works, for a convenient overview, we categorize the reviewed research articles in Table 3 according to the following dimensions:

- **Model.** This column lists the model name and provides the reference to the main paper.

- **Attack and Defense Model.** This column represents the main attack and defense strategies applied on various recommendation models and the attack granularity on the system.

  (1) **Attack model.** Among all attacks strategies proposed in the community of CV [2], in RS the most dominant attack approaches to date have been FGSM and C&W, and attacks based on GANs (see Section 3).

  (2) **Defense model.** As for the best defensive strategy against attack, we have found the strategy adversarial training (a.k.a. adversarial regularization) as the most commonly-adopted approach irrespective of the attack model, while distillation is adopted only by a single paper [37].

  (3) **Attack granularity.** This column represents the level of data on which the adversarial perturbation is added on. It is important to note that while in the computer vision domain, these perturbations are added on raw data (e.g., pixel values), in RS, they are applied on the model parameters.

---

As it can be noted, BPR can be viewed as a classifier on the triple \((u, i, j)\), where the goal of the learner is to classify the difference \(\hat{x}_{ui} - \hat{x}_{uj}\) as correct label +1 for a positive triple sample and 0 for a negative instance.
Table 3. Classification of approaches that address adversarial learning for attacking and defending RS models

<table>
<thead>
<tr>
<th>Model Name</th>
<th>Authors</th>
<th>Year</th>
<th>Attack &amp; Defense Models</th>
<th>Recommendation &amp; Learning</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td>FGSM</td>
<td>GAN-based</td>
</tr>
<tr>
<td>APR [51]</td>
<td>He et al.</td>
<td>2018</td>
<td>✓</td>
<td>✓</td>
</tr>
<tr>
<td>AMR [112]</td>
<td>Tang et al.</td>
<td>2019</td>
<td>✓</td>
<td>✓</td>
</tr>
<tr>
<td>FGACAE [142]</td>
<td>Yuan et al.</td>
<td>2019</td>
<td>✓</td>
<td>✓</td>
</tr>
<tr>
<td>ACAE [141]</td>
<td>Yuan et al.</td>
<td>2019</td>
<td>✓</td>
<td>✓</td>
</tr>
<tr>
<td>FNCF [37]</td>
<td>Du et al.</td>
<td>2019</td>
<td>✓</td>
<td>✓</td>
</tr>
<tr>
<td>ATF [22]</td>
<td>Chen et al.</td>
<td>2019</td>
<td>✓</td>
<td>✓</td>
</tr>
<tr>
<td>GANAtt [29]</td>
<td>Christakopoulos et al.</td>
<td>2019</td>
<td>✓</td>
<td>✓</td>
</tr>
<tr>
<td>AdvIR [86]</td>
<td>Park et al.</td>
<td>2019</td>
<td>✓</td>
<td>✓</td>
</tr>
<tr>
<td>AMASR [114]</td>
<td>Tran et al.</td>
<td>2019</td>
<td>✓</td>
<td>✓</td>
</tr>
<tr>
<td>ATMIRPR [124]</td>
<td>Wang et al.</td>
<td>2020</td>
<td>✓</td>
<td>✓</td>
</tr>
<tr>
<td>SACRA [69]</td>
<td>Li et al.</td>
<td>2020</td>
<td>✓</td>
<td>✓</td>
</tr>
<tr>
<td>TAaMR [36]</td>
<td>Di Noia et al.</td>
<td>2020</td>
<td>✓</td>
<td>✓</td>
</tr>
</tbody>
</table>

parameters of recommendation strategy, as illustrated in Fig. 3. In particular, adversarial perturbations are added to one of the following data: (i) directly on the user profile (i.e., user rating profile), (ii) user and item latent factor model parameters in an LFM, e.g., according to \( p'_u = p_u + \delta, q'_i = q_i + \delta \) in which \( p_u, q_i \in \mathbb{R}^F \) are \( F \)-dimensional embedding factors whose linear interaction explains an unobserved preference; (iii) and (iv) embeddings representing side information of user and items respectively.

- **Recommendation & Learning.** The core recommendation models that we consider in this survey are CBF, CF and CA. We also consider hybrid systems but we do not specify a placeholder for such systems; if an approach use both CBF+CF, we simply mark both corresponding columns, regardless of which hybridization technique it uses [1]. Instead, given the ML (optimization)-based approach for most of the considered papers, we categorize papers based on the recommendation prediction model according to linear LFM (e.g., MF or variations of that such as PMF), linear tensor factorization (TF), non-linear models based on auto-encoder (NL-AE) and neural network (NL-NN); furthermore we classify the loss function used in the core optimization model of the attack and defense scenarios based on BPR [91] and cross-entropy.

Looking at Table 3 globally, we note that adversarial personalized ranking (APR) [51] by He et. al. was the first work that formally addressed AML to improve the robustness of BPR-MF. After this pioneering work, in the following years, a growing number of works have considered application of AML for different recommendation tasks. Another interesting observation is the co-occurrence of the attack type FGSM and defense model adversarial training (AdReg). In fact, the adversarial training procedure based on FGSM is the first defense strategy proposed by Goodfellow et al. [45] to train DNNs resistant to adversarial examples. The authors interpret the improvement in robustness
Table 4. Evaluation and domain comparison of adversarial machine learning approaches for attack and defense on RS (ML: Movielens, FL: FilmTrust, EM: EachMovie, CD: CiaoDVD, Yelp: YE, LFM: LastFM, PI: Pinterest, AM: Amazon, 30M: 30Music, YA: Yahoo, AotM: Art of the Mix)

<table>
<thead>
<tr>
<th>Model Name</th>
<th>Authors</th>
<th>Year</th>
<th>Evaluation</th>
<th>Domain &amp; Dataset</th>
</tr>
</thead>
<tbody>
<tr>
<td>APR [51]</td>
<td>He at al.</td>
<td>2018</td>
<td>✓ ✓ ✓ ✓ ✓</td>
<td>tourism, SM/SN YE, PI, GO</td>
</tr>
<tr>
<td>ACAE [141]</td>
<td>Yuan et al.</td>
<td>2019</td>
<td>✓ ✓ ✓ ✓ ✓</td>
<td>movie ML 1M, CD, FT</td>
</tr>
<tr>
<td>FGACAE [142]</td>
<td>Yuan et al.</td>
<td>2019</td>
<td>✓ ✓ ✓ ✓ ✓</td>
<td>movie ML 1M, CD, FT</td>
</tr>
<tr>
<td>AMR [112]</td>
<td>Tang et al.</td>
<td>2019</td>
<td>✓ ✓ ✓ ✓ ✓</td>
<td>fashion PI, AM</td>
</tr>
<tr>
<td>FNCF [37]</td>
<td>Du et al.</td>
<td>2019</td>
<td>✓ ✓ ✓ ✓ ✓</td>
<td>movie ML (100k, 1M)</td>
</tr>
<tr>
<td>AT [42]</td>
<td>Chen et al.</td>
<td>2019</td>
<td>✓ ✓ ✓ ✓ ✓</td>
<td>movie, music ML, LFM</td>
</tr>
<tr>
<td>GANA [29]</td>
<td>Christakopoulos et al.</td>
<td>2019</td>
<td>✓ ✓ ✓ ✓ ✓</td>
<td>movie ML 1M</td>
</tr>
<tr>
<td>AdVR [86]</td>
<td>Park et al.</td>
<td>2019</td>
<td>✓ ✓ ✓ ✓ ✓</td>
<td>movie ML 100k</td>
</tr>
<tr>
<td>AMASR [114]</td>
<td>Tran et al.</td>
<td>2019</td>
<td>✓ ✓ ✓ ✓ ✓</td>
<td>music 30M, AotM</td>
</tr>
<tr>
<td>ATMBPR [124]</td>
<td>Wang et al.</td>
<td>2020</td>
<td>✓ ✓ ✓ ✓ ✓</td>
<td>tourism, SM/SN, movie ML (100k, 1M), YA, YE, PI</td>
</tr>
<tr>
<td>SACRA [69]</td>
<td>Li et al.</td>
<td>2020</td>
<td>✓ ✓ ✓ ✓ ✓</td>
<td>tourism, SM/SN, business YE, FS</td>
</tr>
<tr>
<td>RAP [4]</td>
<td>Beigi et al.</td>
<td>2020</td>
<td>✓ ✓ ✓ ✓ ✓</td>
<td>movie ML 100k</td>
</tr>
</tbody>
</table>

to adversarial examples because the proposed procedure is based on the minimization of the error on adversarially perturbed data.

Furthermore, in Table 4, we provide an overview of the presented approaches under the perspective of experimental evaluation. In particular, we classify the surveyed works according to the preference score used for building/training the recommender models according to implicit and explicit (i.e., rating-based) feedbacks, the prominent evaluation metrics utilized for the offline evaluation of attack success (NDCG, HR, SuccessRate, F1, distortion, Precision, and MAP), the domain of focus (e.g., movie, music, social media, business) and datasets used for evaluation. We may notice that, most of the approaches have been tested on an implicit preference type. As for the evaluation metrics, HR is the most adopted one followed by nDCC with a partial overlap among approaches adopting them both. As for the application domain of the datasets used for the evaluation, movie is the most adopted one. This is mainly due to the popularity the Movielens datasets (in their two variants 1M and 100k). Interestingly, tourism is an emerging domain thanks to the availability of the Yelp dataset. Finally, we observe that the high majority of the baselines are based on MF approaches. The following section will provide a detailed description of the most prominent approaches.

[APR] He et al. [51] are the first to propose an adversarial learning framework for recommendation. The proposed model, called adversarial personalized ranking (APR), examines the robustness of BPR-MF to adversarial perturbation on users and items embedding of a BPR-MF [91]. The authors verify the success of using adversarial training as a defense strategy against adversarial perturbations and demonstrate the competitive results in applying adversarial training on BPR-MF.

Under Review
Tang et al. [112] put under adversarial framework another BPR model, namely visual-BPR (VBPR). VBPR is built upon BPR and extends it by incorporating visual dimensions (originally based on deep CNN feature) by using an embedding matrix. In [112], the authors first motivate the importance for adversarial training of VBPR by visually depicting how a surprisingly modest amount of adversarial perturbation ($\epsilon = 0.007$) added on raw image pixels — where the added noise is barely perceivable to the human eye — can alter recommendation ranking outcomes of VBPR and produce erroneous results. The proposed model therefore consists of constructing adversarial perturbations under the FGSM attack model and adding them to the deep latent feature of items’ images extracted by CNN (i.e., ResNet50 [49]) with the goal to learn robust image embedding parameters. One of the key insights about this work is that it does not add perturbations directly on raw image pixels for two main reasons: (i) it would require the feature extractor (CNN) component and the recommender model to be trained end-to-end with overfitting issues on the CNN due to the sparsity of user-item feedback data, (ii) it would be a time-consuming operation because at each update of the recommender model it is necessary to update all the CNN parameters.

In the above-mentioned works, the authors adopt several steps to validate the effectiveness of the proposed adversarial training framework, which can be summarized according to the following dimensions: (i) the generalization capability, (ii) the comparison of adversarial noise v.s. random noise, and (iii) the robustness of models. Regarding (i), the key insight is that adversarial training approaches (i.e., APR and AMR) can lead to learning model parameters, which can enhance model generalization capability — in other words, improvement of the general performance of recommendation while not being exposed to adversarial perturbation. Concerning (ii), it has been demonstrated that the impact adversarial perturbation on classical recommendation models (e.g., MF-BPR or VBPR) is significantly larger than their random noise counter-part under similar perturbation level. For instance, [112] shows that by exposing MF to adversarial and random noise, the test on nDCG is decreased by -21.2% and -1.6% respectively — i.e., an impact of approximately 13 times difference. Dimension (iii) constitutes the core of the system validations in these works in which compelling evidence has been provided on the vulnerability of classical recommendation models to adversarial examples, or equivalently the robustness of the proposed training framework against adversarial samples. To provide an illustrating example, in [112] it has been shown for an experiment on the Amazon dataset, that by changing the perturbation level from $\epsilon = 0.05$ to $\epsilon = 0.2$, the amount of decrease in nDCG ranges from -8.7% to -67.7% whereas for AMR it varies from -1.4% to -20.2%. These results suggest that approaches using adversarial learning instead of classical learning act significantly in a more robust way against adversarial perturbations.

In [86], the authors propose a system to address CF recommendation based on implicit feedbacks. The main issue in learning from implicit interaction is characterized by scarcity of negative feedbacks compared with positive ones, regarded as one-class problem. Sampling uniformly from unobserved data, known as negative sampling, has been introduced in prior work to address this issue. The proposed system in [86] is called AdvIR, which entails an adversarial sampling and training framework to learn recommendation models from implicit interactions. The system applies adversarial training on both positive and negative interaction separately, to create informative adversarial positive/negative samples. The proposed adversarial training approach works for both discrete and continuous input by adding the adversarial perturbation directly on the input vector (e.g., one-hot encoding user-id).

Yuan, F. et al. [141, 142] use the adversarial training framework for a neural network-based recommendation model, namely collaborative denoising auto-encoder (CDAE) [133], based on which the authors propose two variations, namely: i) the adversarial
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collaborative auto-encoder (ACAE) and (ii) fine-grained collaborative auto-encoder (FG-ACAE). ACAE applies adversarial noise on encoder and decoder parameters and adopts an adversarial training framework. FG-ACAE considers the impact of adversarial noise in a more fine-grained manner. In particular, in FG-ACAE adversarial noise is added not only on encoder and decoder but also on the user’s embedding matrix as well as hidden layers of the network. Furthermore, to increase the flexibility of training, all the noise factors in ACAE and FG-ACAE are controlled by different parameters. The experimental results confirm the trend that AdReg may improve the model’s robustness against adversarial perturbed input, as well as the generalization performance of recommenders.

[ATF] Chen and Li [22] combine tensor factorization and adversarial learning to improve the robustness of pairwise interaction tensor factorization (PITF) [92] for context-aware recommendation. Comparison with standard tensor models in tag recommendations acknowledges that the adversarial framework outperforms state-of-the-art tensor-based recommenders.

[FNCF] Du et al. [37] approach security issues for C&W attacks [16]. The authors propose to make more robust neural network-based collaborative filtering models (e.g., NCF [52]) by using knowledge distillation [55] instead of the adversarial (re)training. The framework integrates knowledge distillation with the injection of additive adversarial noise at training time. Experiments demonstrate that this system enhances the robustness of the treated recommender model.

[SACRA] Li R. et al. [68] propose a novel recommender model, named Click Feedback-Aware Network (CFAN), to provide query suggestions considering the sequential search queries issued by the user and her history of clicks. The authors employ additional adversarial (re)training epochs (i.e., adding adversarial perturbations on item embeddings) to improve the robustness of the model.

[TAAmR] Di Noia et al. [36] explore the influence of targeted adversarial attacks (i.e., FGSM[45], and PGD [77]) against original product images used to extract deep features in state-of-the-art visual recommender models (i.e., VBPR [50], and AMR [112]). The authors verify that recommendation lists can be altered such that a low recommended product category can be pushed by adding adversarial noise on product images in a human-imperceptible way.

3 ADVERSARIAL LEARNING FOR GAN-BASED RECOMMENDATION

What we presented in Section 2 deals with the class of “discriminative” models where the main aim is to learn the conditional probability \( p(y|x) \). The focus of the current section is on a novel class of “generative” models, named Generative Adversarial Networks (GANs). Loosely speaking, a generative model cares about the generative process behind data —or product features in a recommendation scenario — to categorize the data instances. Here the focus is on learning \( p(x|y) \) from the data.

GANs are a powerful class of generative models that use two networks —trained simultaneously in a zero-sum game— with one network focused on data generation and the other one centered on discrimination. The adversarial learning scheme — or the min-max game — which lies in the heart of GANs empowers these ML models with phenomenal capabilities such as the ability to model high-dimensional distributions. As a result, these networks have been exploited to solve challenging problems in computer vision. The research in RS community has used the generalization (or in technical term data distribution capturing) potential of GANs as an opportunity to solve a variety of tasks relevant to RS.

As it can be noted the term “adversarial” inside generative adversarial networks refers to the learning scheme used by these models and not the application. In other words, the application

Under Review
3.1 Foundations of Generative Adversarial Networks (GANs)

GANs are deep generative models proposed by Goodfellow et al. [44] in 2014. A GAN is composed of two components, a generator $G$, and a discriminator $D$. The generator works to capture the real data distribution to generate adversarial examples and fool the discriminator, while the discriminator endeavors to distinguish the fake examples from real ones. This competition, known as adversarial learning, ends when the components reach the Nash equilibrium. The GAN architecture is shown in Figure 4.

Definition 3.1 (Conventional Vanilla GAN). Assume that we are given a dataset of input samples $x \in \mathcal{X}$, where $\mathcal{P}_X$ represents the probability distribution of the original data and suppose $z \in \mathcal{Z}$ denotes a sample from some latent space $\mathcal{Z}$. We are interested in sampling from $\mathcal{P}_X$. The goal of GAN is to train the generator $G$ to transform samples $z \sim \mathcal{P}_Z$ into $g_\theta(z) \sim \mathcal{P}_\theta$ such that $\mathcal{P}_\theta \approx \mathcal{P}_X$.

$$
\min_\theta \max_\phi L(G_\theta, D_\phi) = \mathbb{E}_{x \sim \mathcal{P}_X} \log f_\phi(x) + \mathbb{E}_{z \sim \mathcal{P}_Z} \log (1 - f_\phi(g_\theta(z)))
$$

where $\theta$ and $\phi$ are model parameters of the discriminator and generator respectively, learned during the training phase.

Different distance measures $f_\theta$ lead to different GAN models, e.g., Vanilla GAN (based on Jensen-Shannon divergence) [44], Wasserstein GAN (based on Wasserstein distance) [3], and Conditional GAN (based on class conditioning on both the generator and discriminator) [81].

Definition 3.2 (Conditional-GAN (CGAN)[81]). Conditional GAN extends the conventional GAN by incorporating an extra condition information term $c$ on both the input of the generator $G$ and
the discriminator $D$, thus conditioning them on this new term

$$\min_{\theta} \max_{\phi} L(G_{\theta}, D_{\phi}) = \mathbb{E}_{x \sim \mathbb{P}_X} \log f_{\phi}(x|c) + \mathbb{E}_{z \sim \mathbb{P}_Z} \log (1 - f_{\phi}(g_{\theta}(z)|c))$$

(13)

where $c$ can represent any auxiliary information to the networks such as class labels, content features, data from other domains and so forth.

### 3.2 GAN-based Recommendation Framework

GANs have been successfully applied in start-of-the-art RS to learning recommendation models. Since the first pioneering GAN-based work IRGAN [125] in 2017, we have witnessed rapid adoption of these network architectures in many traditional and novel applications and domains. In this section, we provide a conceptual framework that will show how GANs are employed in RS domain and shed light on particularities and differences of GAN application in RecSys and ML.

![Fig. 5. A conceptual view of GAN-CF incorporating GAN to address item recommendation task.](image)

**GAN-CF problem formulation and conceptual model.** The prominent recommendation models in the literature that successfully apply GAN [122, 125] for the CF task, utilize the two-player min-max game with objective function built on top of Eq. 13.

**Definition 3.3 (The GAN-CF model).** Let $U$ and $I$ denote a set of users and items in a system, respectively. The training objective is given by

$$\min_{\theta} \max_{\phi} L(G_{\theta}, D_{\phi}) = \mathbb{E}_{i \sim \mathbb{P}_X(i|u)} \log f_{\phi}(i|u) + \mathbb{E}_{i \sim \mathbb{P}_Z(i|u)} \log (1 - f_{\phi}(\hat{i}|u))$$

(14)

where $i \in I$ is an item receiving implicit (or explicit) feedback by user $u \in U$ (e.g., purchased) and $\hat{i} \in I$ is a generated item.

A few observations are important to be made here: (i) the output of generator $G$ is a set of item indices deemed relevant to user $u$; (ii) both $G$ and $D$ are user-conditioned, signifying that model parameters are learnt in a personalized fashion; (iii) the GAN-based CF works do not use the noise term as input (to $G$) as the goal is to generate one unique —yet plausible— item rather than a set of items. Figure 5 summarizes these aspects conceptually.

Under Review
Table 5. Key sampling strategies proposed for CF-GAN recommendation models

<table>
<thead>
<tr>
<th>Method</th>
<th>Key insight</th>
<th>Formal description</th>
</tr>
</thead>
<tbody>
<tr>
<td>REINFORCE* [109]</td>
<td>Optimize $G$ with $K$ discrete items $i_k$.</td>
<td>$\nabla_\theta \approx \frac{1}{K} \sum_{k=1}^{K} \nabla_\theta \log P_\theta(i_k</td>
</tr>
<tr>
<td>Gumbel-Softmax**</td>
<td>Approximate discrete items with virtual items $v_k$ through a differentiable estimator.</td>
<td>$v_k = \exp((\log P_\theta(i_k</td>
</tr>
</tbody>
</table>

* $\nabla_\theta$ is the gradient of the generator $G$.
** In the Gumbel-Softmax formulation $g_k$ and $g_j$ represent sampled noise, and $\tau$ is a temperature hyper-parameter to control the smooth of distribution ($\tau \approx 0$, the probability is concentrated to few items).

Discrete outcome and sampling strategies. The parameters in the GAN-CF model are learned in an end-to-end fashion. However, before we can take benefit of this training paradigm, the system needs to solve a critical issue that does not exist on the original GAN presented in Def. 3.1 based on the sampled noise signal. The generation of recommendation lists is a discrete sampling operation, i.e., performed over discrete candidate items (see Figure 5). Thus, the gradients that are derived from the objective function in Eq. (14) cannot be directly used to optimize the generator via gradient descent as happens in the original GAN formulation, where gradients are applied for differentiable values (e.g., images and videos). To obtain a differentiable sampling strategy in GAN-CF models, two sampling strategies are proposed in the literature based on reinforcement learning algorithm and the Gumbel-Softmax differentiable sampling procedure [58, 108, 109], summarized in Table 5.

3.3 GAN-based Recommendation Models: State of the Art
We have identified a total of 47 papers that integrate GAN in order to accomplish a particular RS-related task, and we classified them according to:

1. Collaborative Recommendation
2. Context-aware Recommendation
3. Cross-domain Recommendation
4. Fashion Recommendation

We present Table 6 to summarize the proposed models and provide insights about the constituting building blocks of the GAN model. From a global perspective, we can see a correlation between the class of $G$, $D$ and the recommendation task. For example, recursive models based on RNN are used for CA Temporal-aware Rec. tasks, areas where these models can better capture the sequence information. This is while, for Collaborative Rec. tasks, the rest of models are commonly used (e.g., Linear LFM, MLP and so on). It is interesting to note that CNN is used for majority of works in Fashion Rec. From a training perspective, we can see that both point-wise and pair-wise models are almost equally used in all these works, perhaps indicating the point-wise training is still a useful method for evaluation of many GAN-based related RS models. In the following, we review each of these application scenarios by describing the most prominent approaches.

3.3.1 Collaborative Recommendation
GANs have been shown powerful in generating relevant recommendations — in particular, using the CF approach — and capable of successively competing with state-of-the-art models in the field of RS. We have identified the following reasons for the potential of GANs in RS: (i) they are able...
to generalize well and learn unknown user preference distributions and thus be able to model user preference in complex settings (e.g., IRGAN [125] and CFGAN [18]); (ii) they are capable of generating more negative samples than random samples in pairwise learning tasks (e.g., APL [108], DASO [39]) and (iii) they can be used for data augmentation (e.g., AugCF [127] and RAGAN [17]).

**[IRGAN]** The work by Wang et. al. [125] is presumably the first attempt to integrate the generative and discriminative approach to IR under the same roof by proposing a GAN-based IR model. The authors demonstrate the application of IRGAN for web search, item recommendation and question answering tasks where for the item recommendation task, the query is constructed from the user’s historical interactions. During adversarial learning—the min-max game—the generator learns the actual distribution of relevant items as much as possible. It turns out that this novel training idea results in a more satisfactory accuracy in recommendation than optimizing the traditional pure discriminative loss functions based on pointwise, or pairwise, objectives.

**[GraphGAN]** In [122], H. Wang et al. propose GraphGAN — a graph-based representation learning — (a.k.a. network embedding) for CF recommendation. Graph-based analysis is gaining momentum in recent years due to their ubiquity in real-world problems such as modeling user preference for item recommendation as well as social graphs in social media (SM) networks, co-occurrence graph in linguistics, citation graph in research, knowledge graph and so forth. The central idea of network embedding is to represent each entity in a graph with a lower-dimensional latent representation to facilitate tasks within the network and prediction over entities. For example, such latent representation makes it possible to perform prediction for supervised tasks, while the distance between node embedding vectors can serve as a useful measure in unsupervised tasks. GraphGAN can be viewed as a graph-based representation of IRGAN, where queries/items are nodes of the graph. For a given node $v_c$, the objective of $G$ is to learn the ground-truth connectivity distribution over vertices $p_{true}(v|v_c)$, whereas $D$ aims to discern whether or not a connectivity should reside between vertex pairs $(v, v_c)$. GraphGan furthermore proposes the graph softmax as $G$—instead of traditional softmax— which appears to boost the computational efficiency of training (graph sampling and embedding learning) performed by $G$.

**[GAN-HNBR]** From an application perspective, GAN-based graph representations have also been applied in more niche domains of RS, including personalized citation recommendation. The goal is to recommend research articles for citation by using a content-based and author-based representation [145] or learning heterogeneous bibliographic network representation (HBNR). In [11] Cai et al. propose GAN-HNBR —a GAN-based citation recommendation model— that can learn the optimal representation of a bibliographic network consisting of heterogeneous vertex content features such as papers and authors into a common shared latent space and provide personalized citation recommendation.

**[CFGAN]** CFGAN has been introduced in [18] to address a problem with discrete items in IRGAN, where $G$ produces at each iteration a single item index, which is a discrete entity in nature. This is different from the original GAN in the CV domain in which the output of $G$ is an image (i.e., a vector). The generation of discrete item indices by $G$ results in a poor sampling of items from the pool of available alternatives (i.e., samples identical to ground-truth) deteriorating the performance of $G$ and $D$—instead of improvement— during the min-max training iteration. CFGAN introduces vector-wise training in which $G$ generates continuous-valued vectors to avoid misleading $D$, which in turn improves the performance of both $G$ and $D$. The authors show the improvement of CFGAN over IRGAN and GraphGAN baselines. As an example, with regards to P@20 on the Ciao dataset, the improvement is 100% for CFGAN vs. IRGAN (0.45 v.s. 0.23) and 160% for CFGAN vs. GraphGAN (0.45 v.s. 0.17), which turns to be a significant improvement of the recommendation accuracy.
Table 6. A schematic representation of GAN-based approaches to recommendation.

<table>
<thead>
<tr>
<th>Model Name</th>
<th>Year</th>
<th>Generator ($\mathcal{G}$)</th>
<th>Discriminator ($\mathcal{D}$)</th>
<th>Training</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>Linear LFM</td>
<td>MLP</td>
<td>CNN</td>
</tr>
<tr>
<td>Collaborative Rec.</td>
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<td></td>
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<tr>
<td>IRGAN [125]</td>
<td>2017</td>
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<td></td>
<td></td>
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<tr>
<td>CFGAN [138]</td>
<td>2018</td>
<td>✓</td>
<td></td>
<td></td>
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<tr>
<td>Chae et al. [19]</td>
<td>2018</td>
<td>✓</td>
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<tr>
<td>AVAE [143]</td>
<td>2018</td>
<td>✓</td>
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<tr>
<td>CAAE [20]</td>
<td>2019</td>
<td>✓</td>
<td></td>
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<tr>
<td>CGAN [113]</td>
<td>2019</td>
<td>✓</td>
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<td>CALF [30]</td>
<td>2019</td>
<td>✓</td>
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<tr>
<td>PD-GAN [132]</td>
<td>2019</td>
<td>✓</td>
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<tr>
<td>LambdaGAN [128]</td>
<td>2019</td>
<td>✓</td>
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<tr>
<td>VAEGAN [139]</td>
<td>2019</td>
<td>✓</td>
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<td>APL [108]</td>
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<tr>
<td>RsyGAN [137]</td>
<td>2019</td>
<td>✓</td>
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<tr>
<td>CoFGAN [73]</td>
<td>2020</td>
<td>✓</td>
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<tr>
<td>Graph-based Collaborative Rec.</td>
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<tr>
<td>GraphGAN [122]</td>
<td>2018</td>
<td>✓</td>
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<td></td>
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<tr>
<td>VCGAN [145]</td>
<td>2018</td>
<td>✓</td>
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<tr>
<td>UPGAN [48]</td>
<td>2020</td>
<td>✓</td>
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<tr>
<td>Hybrid Collaborative Rec.</td>
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<tr>
<td>VAE-AR [66]</td>
<td>2017</td>
<td>✓</td>
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<tr>
<td>RGD-TR [71]</td>
<td>2018</td>
<td>✓</td>
<td></td>
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<tr>
<td>aae-RS [136]</td>
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<td>✓</td>
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<tr>
<td>SDNet [26]</td>
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<tr>
<td>ATR [89]</td>
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<tr>
<td>AugCF [127]</td>
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<td>✓</td>
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<tr>
<td>RSGAN [138]</td>
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<td>✓</td>
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<tr>
<td>RRGAN [24]</td>
<td>2019</td>
<td>✓</td>
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<tr>
<td>UGAN [129]</td>
<td>2019</td>
<td>✓</td>
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<tr>
<td>LARA [107]</td>
<td>2020</td>
<td>✓</td>
<td></td>
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<tr>
<td>CGAN [28]</td>
<td>2020</td>
<td>✓</td>
<td></td>
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<tr>
<td>Context-aware Rec.</td>
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<tr>
<td>Temporal-aware</td>
<td></td>
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<tr>
<td>RecGAN [8]</td>
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<td>NMRN-GAN [126]</td>
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<td>✓</td>
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<td>AAE [116]</td>
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<tr>
<td>PLASTIC [147]</td>
<td>2018</td>
<td>✓</td>
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<tr>
<td>LSIC [146]</td>
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<tr>
<td>Geo-ALM [75]</td>
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<td></td>
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<tr>
<td>APOIR [148]</td>
<td>2019</td>
<td>✓</td>
<td></td>
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<tr>
<td>Cross-domain Rec.</td>
<td></td>
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<tr>
<td>VAE-GAN-CC [82]</td>
<td>2018</td>
<td>✓</td>
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<tr>
<td>RecSys-DAN [121]</td>
<td>2019</td>
<td>✓</td>
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<td>FR-DiscoGAN [59]</td>
<td>2019</td>
<td>✓</td>
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<td>DASO [39]</td>
<td>2019</td>
<td>✓</td>
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<td>CnGAN [88]</td>
<td>2019</td>
<td>✓</td>
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<tr>
<td>Fashion Rec.</td>
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<td>DVBPR [60]</td>
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<td>CRAFT [57]</td>
<td>2018</td>
<td>✓</td>
<td></td>
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<tr>
<td>MrCGAN [105]</td>
<td>2018</td>
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<tr>
<td>Yang et al. [135]</td>
<td>2018</td>
<td>✓</td>
<td></td>
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<tr>
<td>cGAN [64]</td>
<td>2019</td>
<td>✓</td>
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</tbody>
</table>

Under Review
[Chae et al.] In [19], Chae et al. propose an auto-encoder-based GAN, in which an auto-encoder (AE) is used as $G$ to model the underlying distribution of user preferences over items. The primary motivation behind this work is that conventional MF-based approaches are linear. Instead, the proposed system can generate non-linear latent factor models and uncover more complex relationships in the underlying user-item interaction matrix.

[VAE] An adversarial variational auto-encoder (VAE) is adopted in [143], where the authors propose the usage of a GAN to regularize the VAE by imposing an arbitrary prior to the latent representation (based on implicit feedback). Similar works can be found in [66, 113], which exploits a VAE to enhance the robustness of adversarial examples. The authors furthermore present the Wasserstein distance with gradient penalty.

[CALF] Other issues of IRGAN, such as sparsity causing gradient vanishing and update instability and discrete value preventing a training to optimize using gradient descent, are addressed in [30]. The proposed solution is named convolutional adversarial latent factor model (CALF), which employs a CNN to learn correlations between embeddings and Rao-Blackwell sampling to deal with discrete values optimizing CALF.

[PD-GAN] The authors of [132] propose a solution to improve diversity of CF-based recommendation with GAN based on personalized diversification.

[LambdaGAN] In [128], the authors propose LambdaGAN—a GAN model with a lambda ranking strategy—that improves the recommendation performance in a pairwise ranking setting by proposing lambda rank [140] function into the adversarial learning of the proposed GAN-based CF framework.

[VAEGAN] A variant of VAE is introduced in [139] to address the limited expressiveness of the inference model and latent features, which reduces the generalization performance of the model. The proposed solution, named adversarial variational autoencoder GAN (VAEGAN), is a more expressive, and flexible model that better approximates the posterior distribution by combining VAEs and GAN. This work is one of the first work to propose the application of adversarial variational Bayes (AVB) [79] to perform the adversarial training.

### 3.3.2 Context-aware Recommendation

Although long-term preference modeling has proven to be effective in several domains [6], recent research indicates that users’ preferences are highly variable based on the user’s context, e.g., time, location, and mood [61]. Context provides the background of user objective for using the system and can be exploited to generate more relevant recommendations.

**Temporal-aware Recommendation.** In real applications, users’ preferences change over time, and modeling such temporal evolution is needed for effective recommendation. While long-term preferences of users change slowly, their short-term preferences can be seen as more dynamic and changing more rapidly. Predicting short-term user preference has been recently studied in the context of session-based and sequential recommendations. A temporal extension of SVD++ towards the modeling of temporal dynamic, named TimeSVD++, has been proposed in [62]. It has also been reported that the structure of time-aware inputs (e.g., click-logs, session) are effectively modeled by a recurrent neural network (RNN). For instance, Hidasi et al. [53] proposed to model the sequential user clicks to output session-based recommendation with a GRU-gated recurrent unit; while Wu et al. [131] proposed to integrate an LSTM model, to capture both the user and the item temporal evolution, and MF to model stationary preferences. Inspired by the accuracy
improvements of IRGAN, GAN-based models have been combined in temporal frameworks to boost the recommendation performance in sequence-aware recommendation tasks.

[RecGAN] In [8], the authors propose to incorporate in a single framework both the temporal modeling capabilities of RNN and the latent feature modeling power of the min-max game. The proposed framework, named RecGAN, implements both the generator and the discriminator with the Gated Recurrent Unit (GRU) [27], in order to make \( G \) capable of predicting a sequence of relevant items based on the dynamic evolution of user’s preferences.

[PLASTIC & LSIC] Differently from RecGAN that implements only an RNN cell to capture the dynamic evolution of the user’s behavior, Zhao et al. [146, 147] propose to combine MF and RNN in an adversarial recommendation framework to model respectively long and short-term user-item associations. The proposed framework, named PLASTIC, adopts MF and LSTM cells into \( G \) to account for the varying aspect of both users and items, while a two-input Siamese network—built manually by using a MF and RNN— as \( D \) encodes both the long-term and session-based information in the pair-wise scenario.

[NMRN-GAN] Recent studies have endorsed that adversarially created close-to-observed negative samples are capable of improving the user and item representation. In [126], Wang et al. introduce GAN-based negative sampling for streaming recommendation. Instead of using a random sampling strategy, which is static and hardly contributes towards the training of the recommender model, adversarially generated negative samples result more informative. NMRN-GAN uses a key-value memory network [144] to keep the model’s long-term and short-term memory combined with a GAN-based negative sampling strategy to create more instructive negative samples thus improving the training effectiveness and the quality of the recommendation model.

[GAN-CQDN] A GAN-based solution has been proposed in [25] for sequence-aware recommendation in conjunction with reinforcement learning (RL). The main aim here is that of modeling the dynamic of user’s status and long-term performance. The authors propose GAN-CQDN, an RL-based recommender system that exploits GAN to model user behavior dynamics and learn her reward function. The advantages of using GAN is that it improves the representation of the user profile as well as the reward function according to the learned user profile, and it accommodates online changes for new users.

Geographical-aware Recommendation. Another relevant application of contextual information is point-of-interest (POI) recommendation. In this field, many approaches have been proposed over the year especially after the mobile revolution. Location-based social networks (LBSNs) have attracted millions of users to share rich information, such as experiences and tips. Point-of-Interest (POI) recommender systems play an important role in LBSNs since they can help users explore attractive locations as well as help social network service providers design location-aware advertisements for Point-of-Interest.

[Geo-ALM] In [75], the authors propose Geo-ALM, a GAN-based POI recommender that integrates geographical features (POI and region features) with a GAN to achieve (better) POI recommendation. In the proposed system, \( G \) improves the random negative sampling approach in the pairwise POI recommendation scenario that leads to better representation of user and items and enhances recommendation quality with respect to state-of-the-art models.

[APOIR] Inspired by the advances of POI recommendation performance under GAN-based framework, Zhou et al. propose adversarial point-of-interest recommendation (APOIR) [148] to learn user-latent representations in a generative manner. The main novelty of the proposed framework
is the use of POIs’ geographical features and the users’ social relations into the reward function used to optimize the $G$. The reward function acts like a contextual-aware regularizer of $G$, that is the component of APOIR in the proposed POI recommendation model.

### 3.3.3 Cross-domain Recommendation

Recommender models are usually designed to compute recommendations for items belonging to a single domain. Items belonging to a specific domain share characteristics and attributes, which are intrinsically similar, and domain-specific recommendation models allow the designer to study these characteristics individually. However, single-domain recommendation faces numerous challenges. The first challenge refers to the well-known cold-start problem, when insufficient interactions exist in the considered domain. Second, users’ interests and needs span across different application areas and large e-commerce sites, like Amazon or eBay, store users’ preference scores related to products/services of various domains—from books and products to online movies and music. As companies strive to increase the diversity of products or services to users, cross-domain recommendation can help such companies to increase sales productivity by offering personalized cross-selling or bundle recommendations for items from multiple domains [12]. The third aspect is a novel research idea related to discovering relationships between items (e.g., images) of two different domains. For example, can a machine achieve a human-level understanding to recommend a fashion item consistent with user taste/style in another domain such as media or visual scenery? 

**[FR-DiscoGAN]** In [59], the authors propose a cross-domain GAN to generate fashion designs from the sceneries. In the proposed hypothetical scenario, the user can specify via a query her POI to visit (e.g., mountain, beach) together with keywords describing a season (i.e., spring, summer, fall, and winter). The core idea is to automatically generate fashion items (e.g., clothes, handbags, and shoes) whose useful features (i.e., style) match the natural scenery specified by the user. For instance, the system can recommend a collection of fashion items that look cool/bright for visiting a beach in summer, even though the actual preference of the user is black-style clothes. The role of GAN is to learn associations between scenery and fashion images. In the field of ML and CV, the problem is termed as "style transfer" or "image to image translation" problem [41].

**[VAE-GAN-CC]** An effective cross-domain recommendation system relies on capturing both similarities and differences among features of domains and exploiting them for improving recommendation quality in multiple domains. Single-domain algorithms have difficulty in uncovering the specific characteristics of each domain. To solve this problem, some approaches extract latent features of the domains by a separate network [72, 80]. Although these approaches might be successful in capturing characteristic features of each domain, they do not establish the similarity between features of multiple domains. To extract both homogeneous and divergent features in multiple domains, in [82] Nguyen et al. propose a generic cross-domain recommendation system that takes as input the user interaction history (click vector) in each domain, maps the vectors to a shared latent space using two AEs and then uses $G$ to remap the underlying latent representation to click vectors. The main novelty of this work lies in building/linking shared latent space between domains, which in turn facilitates domain-to-domain translation. In particular, the former is realized by enforcing a weight-sharing constraint related to variational auto-encoders, i.e., the encoder-generator pair \{$E_A, G_A$\} and \{$E_B, G_B$\} and using cycle-consistency (CC) as a weight-sharing constraint. Finally, two separate adversarial discriminators are employed to determine whether the translated vectors are realistic. The final system is called VAE-GAN-CC network, which extends the unsupervised image-to-image translation network in the CV domain [74] for RS applications and is thus named domain-to-domain translation model (D2D-TM).
[DASO] Inspired by the efficacy of adversarial negative sampling techniques proposed in [126], Fan et al. [39] address the limitation of typical negative sampling in the social recommendation domain in transferring users’ information from social domain to item domain. The proposed Deep Adversarial SOcial recommendation (DASO) system, harnesses the power of adversarial learning to dynamically generate difficult negative samples for user-item and user-user pairs, to guide the network to learn better user and item representations. The authors validate the effectiveness of the system compared with the state-of-the-art pairwise ranking and GAN-based models.

[CnGAN] Perera et al. in [88], propose GAN for cross-network (CnGAN) to address one of the significant shortcomings of cross-network recommendation concerning non-overlapping users missing preference scores. These users exist in the source domain but not in the target domain, and thus, their preferences about items in the target domain are not available. In the proposed work, \( G \) learns the mapping of user preferences from target to source and generate more informative preferences on the source domain. \( D \) uses the synthetically generated preferences (generated from \( G \)) to provide recommendations for users who only have interactions on the target network (not overlapped users). The authors also propose two novel loss functions—a content-wise and a user-wise loss function—to guide the min-max training process better. The authors validate the effectiveness of the system against state-of-the-art models both in terms of accuracy and beyond-accuracy measures (novelty, diversity).

### 3.3.4 Fashion Recommendation

Most conventional RS are not suitable for application in the fashion domain due to unique characteristics hidden in this domain. For instance, people do not follow the crowd blindly when buying clothes or do not buy a fashion item twice [100]. Another aspect is related to the notion of complementary relationship for recommending a personalized fashion outfit. It is natural for humans to establish a sense of relationship between products based on their visual appearance. Recently, GAN-based models have shown promising performance for outfit recommendation, being able to compete with state-of-the-art fashion recommendation models in the field, such as Siamese-base networks [40]. Finally, another new application of GANs is related to exploiting the generative power of GANs to synthesize real-looking fashion clothes. This aspect can inspire the aesthetic appeal/curiosity of costumer and designers and motivates them to explore the space of potential fashion styles.

[CRAFT] Huynh et al. [57] address the problem of recommending complementary fashion items based on visual features by using an adversarial process that resembles GAN and uses a conditional feature transformer as \( G \) and a discriminator \( D \). One main distinction between this work and the prior literature is that the \( \langle \text{input, output} \rangle \) pair for \( G \) are both features (here features are extracted using pre-trained CNNs [110]), instead of \( \langle \text{image, image} \rangle \) or hybrid types such as \( \langle \text{image, features} \rangle \) explored in numerous previous works [119, 150]. This would allow the network to learn the relationship between items directly on the feature space, spanned by the features extracted. The proposed system is named complementary recommendation using adversarial feature transform (CRAFT) since in the model, \( G \) acts like a feature transformer that—for a given query product image \( q \)— maps the source feature \( s_q \) into a complementary target feature \( \hat{t}_q \) by playing a min-max game with \( D \) with the aim to classify fake/real features. For training, the system relies on learning the co-occurrence of item pairs in real images. In summary, the proposed method does not generate new images; instead it learns how to generate features of the complementary items conditioned on the query item.

[DVBPR] Deep visual Bayesian personalized ranking (DVBPR) [60] is presumably one of the first works that exploit the visual generative power of the GAN in the fashion recommendation
domain. It aims at generating clothing images based on user preferences. Given a user and a fashion item category (e.g., tops, t-shirts, and shoes), the proposed system generates new images —i.e., clothing items— that are consistent with the user’s preferences. The contributions of this work are two-fold: first, it builds and end-to-end learning framework based on the Siamese-CNN framework. Instead of using the features extracted in advance, it constructs an end-to-end system that turns out to improve the visual representation of images. Second, it uses a GAN-based framework to generate images that are consistent with the user’s taste. Iteratively, \( G \) learns to generate a product image integrating a user preference maximization objective, while \( D \) tries to distinguish crafted images from real ones. Generated images are quantitatively compared with real images using the preference score (mean objective value), inception score [97], and opposite SSIM [84]. This comparison shows an improvement in preference prediction in comparison with non-GAN based images. At the same time, the qualitative comparison demonstrates that the generated images are realistic and plausible, yet they are quite different from any images in the original dataset —they have standard shape and color profiles, but quite different styles.

[MrCGAN] Shih et al. [105] propose a compatibility learning framework that allows the user to visually explore candidate compatible prototypes (e.g., a white T-shirt and a pair of blue-jeans). The system uses metric-regularized conditional GAN (MrCGAN) to pursue the item generation task. It takes as the input a projected prototype (i.e., the transformation of a query image in the latent "Compatibility Space"). It produces as the output a synthesized image of a compatible item (the authors consider a compatibility notion based on the complementary of the query item across different catalog categories). Similar to the evaluation protocol in [57], the authors conduct online user surveys to evaluate whether their model could produce images that are perceived as compatible. The results show that MrCGAN can generate compatible and realistic images under compatibility learning setting compared to baselines.

[Yang et al. & c+GAN] Yang et al. [135] address the same problem settings of MrCGAN [105] by proposing a fashion clothing framework composed of two parts: a clothing recommendation model based on BPR combined with visual features and a clothing complementary item generation based GAN. Notably, the generation component takes in input a piece of clothing recommended in the recommendation model and generates clothing images of other categories (i.e., top, bottom, or shoes) to build up a set of complementary items. The authors follow a similar qualitative and quantitative evaluation procedure as DVBPR [60] and further propose a compatibility index to measure the compatibility of the generated set of complementary items. A similar approach has also been proposed in c+GAN [64], to generate bottom fashion item paired with a given top item.

4 SUMMARY AND FUTURE DIRECTIONS
In this paper, we have surveyed a wide variety of tasks in which adversarial machine learning (AML) is important to attack/defense a recommendation model as well as improve the generalization performance of the model itself. This broad range of applications can be categorized into two —objective-wise distinct— technologies: (i) AML for improving security (cf. Section 2) and, (ii) AML used in generative adversarial networks (GANs) exploited for numerous tasks such as better CF recommendation, context-aware recommendation, cross-domain system, or visually-aware fashion item/outfit recommendation (cf. Section 3). The common point of both technologies is the joint min-max optimization used for training models, in which two competing players play a zero-sum differential game until they reach an equilibrium. To the best of our knowledge, this is the first work that sums up the advances of AML application in recommendation settings and proposes a clear taxonomy to classify such applications.
We put forward what is better to invest in AML-RS research and introduce the following open research directions:

**Bridging the gap between attack/defense models in the ML/CV and RS domain.** As the prior literature of AML for security emerged in the field of machine learning (ML) and computer vision (CV), there remains a large gap between advances made in those fields and that in RS. Consider the questions: “Attacks for images are designed to be human-imperceptible or inconspicuous (i.e., may be visible but not suspicious). How can we capture these notions for designing attacks in RS?”; furthermore, “Images are continuous-valued data while a user profile is a discrete data. Modifying users’ profiles completely changes the semantic of their behaviors. What is the best approach to treat these nuances in RS attack designs?”

**Choice of recommendation models.** Modern recommendation models exploit a wealth of side-information beyond the user-item matrix such as social-connections, multimedia content, semantic data, among others. However, most of the attacks against recommendation systems are designed and validated against CF systems. Investigating the impact of adversarial attacks against these—heterogeneous in nature—data types remains as an open highly interesting challenge, e.g, consider adversarial attacks against music, image, and video recommendation models leveraging multimedia content. In this regard, we also recognize attack against state-of-the-art deep and graph-based models, another highly-valued research direction.

**Definition of attack threat model.** The research in RS community misses a common evaluation approach for attacking/defending scenarios such as the one introduced by Carlini at el. [13]. For instance, it is important to define a common attacker threat model to establish in advance the attacker knowledge and capabilities to make the attack (or defense) reproducible and comparable with novel proposals.

**Move the attention towards beyond accuracy goal in recommendation.** According to our survey, most of the identified research works focus on accuracy metrics such as HR and nDCG. Consider the question: “What is the impact of adversarial attacks and defenses in other evaluation objectives of RS, for instance, diversity, novelty, and fairness of recommendations”. The impact on these metrics could be, in principle, the main objective of a new breed of attack strategies aiming at compromise the diversity/novelty of results.

**Scalability and stability of learning.** We identify that there exists the need to further explore the stability learning problems in the discrete item sampling strategy to train the generator. This has been already identified as a big problem when GAN-based RS are applied in real scenarios with huge catalogues. A point of study may be that of novel GAN models proposed in computer vision (e.g., WGAN [3], LSGAN [78], and BEGAN [7]).

**Users preferences learning with GANs.** An interesting and already established application of AML-RS is to exploit the generative power of GANs to produce more plausible user-rating profiles that can be used to improve recommendations in the cold-user scenario or improve the prediction performance in warm-start settings. We consider such applications extremely interesting, and we motivate further research in this direction to resolve the well-known cold-start obstacles in recommendation settings.

REFERENCES


Under Review


Adversarial Machine Learning in Recommender Systems


